

---

Victoria Linear Collider Workshop, 2004

---

DETERMINATIONS OF THE  $HWW$  AND  $HZZ$   
COUPLINGS AT THE LHC AND AT A LC.

Edmond L. Berger  
Argonne National Laboratory  
July 29, 2004

1. Introduction & Motivation
2. Production Dynamics and WBF Cuts at the LHC
3. Signal Purity and Coupling Uncertainties at the LHC
4. Comparisons with LC estimates
5. Summary

## Introduction and Motivation

---

- Assume a SM-like Higgs boson has been discovered,  $115 < m_H < 200$  GeV at the Tevatron or the LHC, and that a sample exists of  $H + 2$  jet events at the LHC
- Want to use these data to determine the Higgs boson couplings  $g$  to weak vector bosons,  $W$  and  $Z$
- Focus on two production subprocesses that contribute to  $H + 2$  jet events:
  - $W + W \rightarrow H$  and  $Z + Z \rightarrow H$  “WBF”
  - $g + g \rightarrow H$  “irreducible QCD background”
- Issue for the determination of couplings: How well can we resolve WBF production of  $H$  from QCD production of  $H$ ?
- Independent calculation of  $H + 2$  jet processes
  - to gauge the effectiveness of cuts used to select the WBF signal, and
  - to evaluate the accuracy with which coupling  $g$  can be determined in experiments at the CERN LHC

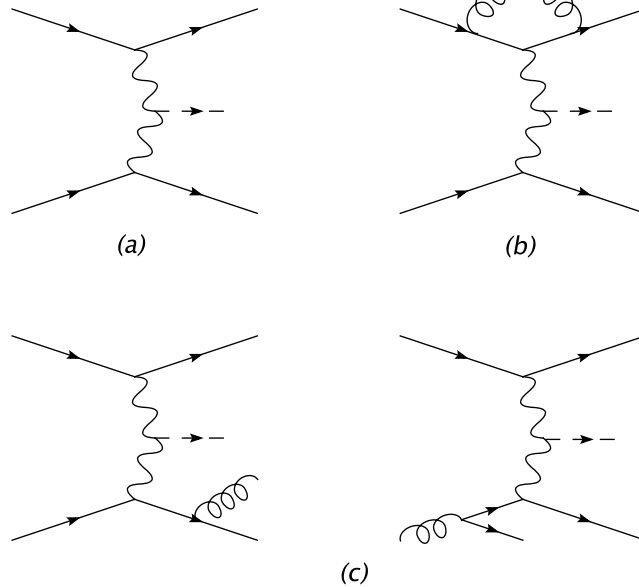
## Introduction and Motivation (continued)

---

- Define Purity  $P = \frac{S}{S+B}$   
 $S$  is the number of signal  $H + 2$  jet events and  
 $B$  is the number of  $H + 2$  jet QCD background events  
both in the WBF region of phase space
- Study Purity  $P$  of the signal vs  $p_T$  of the jets
- Evaluate uncertainty  $\frac{\delta g}{g}$  of the coupling in terms of  
 $P \quad \frac{\delta N}{N} \quad \frac{\delta S}{S} \quad \text{and} \quad \frac{\delta B}{B}$

## $H + 2$ Jet Production – Signal

- Higgs boson  $H$  production via  $WW$  scattering in NLO QCD. Ex:

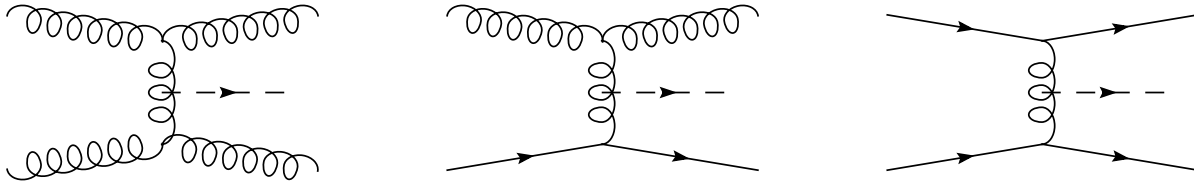


- QCD NLO calculation of  $H + 2$  jets with CTEQ6M parton densities; renormalization/factorization scale  $\mu = m_H$
- Hard perturbative scale  $\mu$  dependence  $\sim 2\%$  for  $\frac{1}{2}m_H < \mu < 2m_H$ , and CTEQ PDF uncertainty  $\sim 3\%$ , both in the WBF region of phase space  
 $\rightarrow$  signal is calculated fairly reliably
- Events generated with the MCFM code  
J. Campbell & R. K. Ellis PRD65,113007 (2002)
- Independent results (dipole subtraction method) verify the NLO calculation of Figy, Oleari, Zeppenfeld, PRD68, 073005 (2003).  
 $K$ -factor  $\sim 10\%$ , with small variation over the phase space appropriate for the WBF signal

## $H + 2$ Jet Production – Irreducible Background

---

- Higgs boson  $H$  production via  $gg$  scattering. Ex:



- Fully differential NLO calculation of  $H + 2$  jet production does not exist; contribution computed at LO Kauffman Desai and Risal, PRD55, 4005 (1997); PRD58, 119901 (1998)
- Effective  $ggH$  coupling included in the limit of  $m_H \ll 2m_t$  and  $p_T^H < m_t$   
(c.f. Del Duca et al NP B616, 367 (2001))
- NLO enhancement ( $K$ ) factor is needed in the region of the WBF cuts. It can be estimated from
  - inclusive NLO  $gg \rightarrow H$   $K \sim 1.7 - 1.8$   
Harlander & Kilgore PRD64, 013015 (2001); Anastasiou & Melnikov, NP B646, 220 (2002)
  - NLO  $gg \rightarrow H + 1$  jet  $K \sim 1.3 - 1.5$   
Ravindran, Smith, van Neerven NP B665, 325 (2003)
- Uncertainty: hard scale  $\mu$  dependence .....

## Event Characteristics

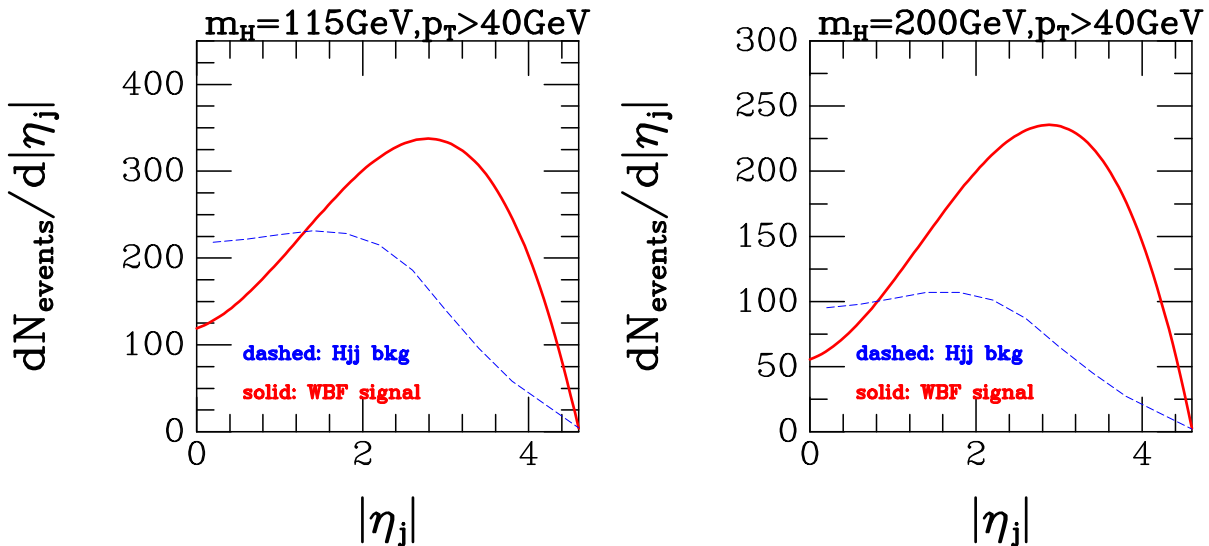
---

- Hallmark of WBF events in hadron reactions is a Higgs boson accompanied by two “tagging” jets having large  $p_T \sim \mathcal{O}(\frac{1}{2}M_W)$
- QCD  $gg \rightarrow H + 2$  jets generate a softer  $p_T$  spectrum
- The rapidity spectra for the WBF and QCD production mechanisms also differ, related to the fact that the gluon parton density (that plays a dominant role in the background) is softer than the quark density; figures shown on next slide
- The  $p_T$  spectrum of the Higgs boson is also relatively hard. All-orders resummed calculation Berger and Qiu PRD 67, 034026 (2003) provides  $\langle p_T^H \rangle \sim 35$  GeV at  $m_H = M_Z$ , growing to  $\langle p_T^H \rangle \sim 54$  GeV at  $m_H = 200$  GeV
- Require reliable QCD representation of  $Hjj$  for jets at large  $p_T$ . Hard matrix elements are needed. A showering approach for generating the momentum distributions of the jets would not suffice; showering yields softer jets and overestimates signal purity

## $H + 2$ Jet Production – Jet Rapidity Distribution

- Higgs boson  $H$  production via  $WW$  and  $ZZ$  scattering in NLO and via  $gg$  QCD processes (LO)

(for  $1 \text{ fb}^{-1}$ , no BR included):



- Shape of the **signal** distribution depends very little on the Higgs boson mass or on the  $p_T$  cut for the tagging jets.

**Peak at  $|\eta| \sim 3$ . Full width at half-max  $\sim 2.8$**

- Background falls off sharply beyond  $|\eta| \sim 2$
- Motivates a **simple WBF prescription**:

$$\eta_{\text{peak}} - \eta_{\text{width}}/2 < |\eta_j| < \eta_{\text{peak}} + \eta_{\text{width}}/2$$

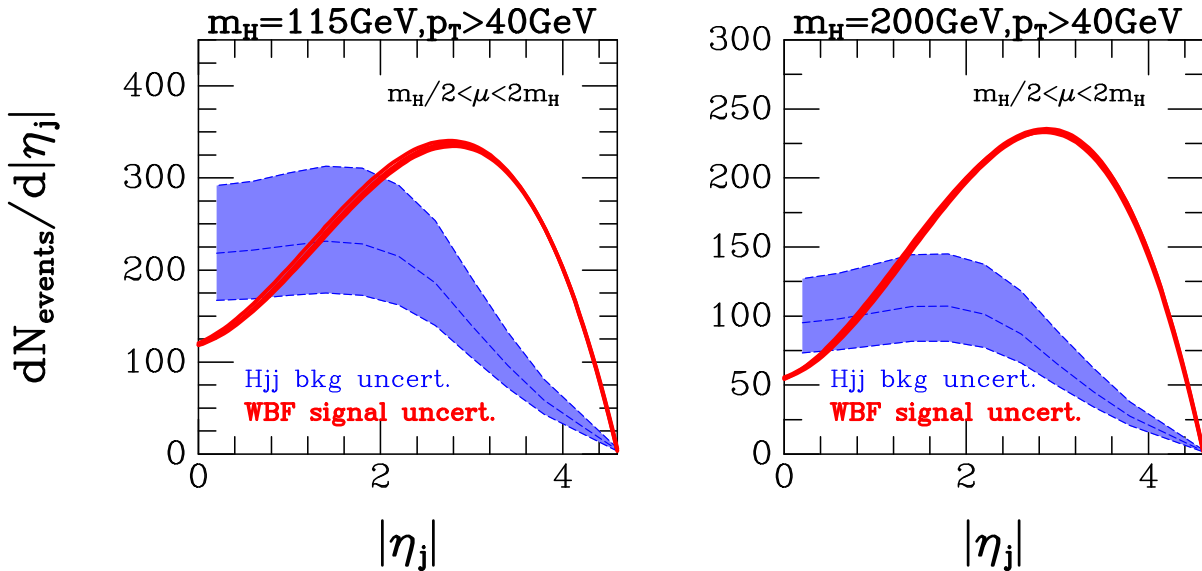
$$j = j_1 \text{ or } j = j_2, \quad \eta_{\text{peak}}=3, \quad \text{and } \eta_{\text{width}}=2.8$$

- This is our working definition of the WBF region

## $H + 2 \text{ Jet Production} - \mu \text{ dependence}$

- Higgs boson  $H$  production via  $WW$  scattering in NLO and via  $gg$  QCD processes (LO)

hard-scale  $\mu$  variation from  $\mu = m_H/2$  to  $\mu = 2m_H$ :



- Magnitude and shape of the **signal** distribution depend very little on  $\mu$ :  $\pm 2\%$
- Magnitude of the background shows significant uncertainty at LO; it is 70% greater at  $\mu = m_H/2$ , and 40% less at  $\mu = 2m_H$
- This uncertainty in the irreducible background translates into uncertainty in the extraction of the coupling strengths. To reduce the uncertainty, a differential NLO calculation is needed for the QCD background process  $H + 2 \text{ jets}$



## $H + 2 \text{ Jet Production} - \text{Event Rates for } 1 \text{ fb}^{-1}$

---

- Event rates for the  $Hjj$  WBF signal(NLO) and  $Hjj$  background(LO), including our WBF requirement that at least one jet have  $1.6 < |\eta| < 4.4$  (no BR included)

$p_T$ cut [GeV]	20	40	80
Signal ( $m_H = 115$ )	1374	789	166
Bkg	1196	382	92
Purity	0.53	0.67	0.64
Signal ( $m_H = 200$ )	928	545	121
Bkg	534	179	46
Purity	0.63	0.75	0.72

- Recall  $P = S/(S + B)$ 
  - Purity is independent of total integrated luminosity
- $p_T$  cut of 40 GeV yields a good S/B across the range  $m_H = 115\text{--}200$  GeV.  $p_T$  cut of 20 GeV is marginal
- Signal purities of  $\sim 65\%$  for  $p_T$  cut  $\gtrsim 40$  GeV; purity is greater at the larger values of  $m_H$

## $H + 2$ Jets – Derivation of Coupling Uncertainty

---

- Both the signal (S) and the background (B) have  $H + 2$  jets;  $N$  = total number of  $H + 2$  jets observed
- Want the uncertainty  $\delta g/g$  on the coupling of the Higgs boson to vector bosons
- Define  $r = g_{\text{observed}}^2 / g_{\text{predicted}}^2 \rightarrow r = \frac{(N-B)}{S}$

- Uncertainty in  $r$ :

$$\delta r / r = \sqrt{(\delta S / S)^2 + ((\delta N)^2 + (\delta B)^2) / (N - B)^2}$$

- In terms of purity  $P = S / (S + B)$

$$\frac{\delta g}{g} = \frac{1}{2} \sqrt{\left(\frac{\delta S}{S}\right)^2 + \frac{1}{P^2} \left(\frac{\delta N}{N}\right)^2 + \frac{(1 - P)^2}{P^2} \left(\frac{\delta B}{B}\right)^2}$$

- Factor  $1/P$  that multiplies  $\delta N/N \rightarrow$   
 $P < 1$  dilutes statistical power of data
- Factor  $(1 - P)/P$  that multiplies  $\delta B/B \rightarrow$   
 $P \rightarrow 1$  reduces role of uncertainty in  $B$
- Size of background is included in  $P$

## Estimates of Uncertainties in $S$ , $B$ , and $N$

---

- Let  $\delta S/S = 5\%$

NLO effects are known;  $\mu$  dep and PDF uncert are estimated

- Let  $\delta B/B = 30\%$

NLO effects not calculated yet for  $H + 2$  jets;  $\mu$  dep of the **NLO inclusive** process is  $\sim 20\%$  for  $\frac{1}{2}m_H < \mu < 2m_H$ ; PDF another  $\sim 5\%$

- For  $N$  and  $\delta N/N$ , we must specify decay modes of  $H$

- for  $m_H = 115$  GeV, pick  $H \rightarrow \tau^+ \tau^-$   
with one  $\tau$  decaying to hadrons and one to leptons  
combined branching ratio 0.033; use hadronic tagging  
efficiency 0.26; net reduction factor  $\epsilon \sim 0.01$
- for  $m_H = 200$  GeV, pick  $H \rightarrow W^+ W^-$ ; if both  
decay to leptons,  $\epsilon \sim 0.036$

- “**Low luminosity**” minimum of  $\sim 10 \text{ fb}^{-1}$  integrated  
luminosity is needed to discover  $H$  in the WBF process

ATLAS, S. Asai et al hep-ph/0402254 **one (good) year of LHC**  
**operation at  $10^{33} \text{ cm}^{-2} \text{ s}^{-1}$**

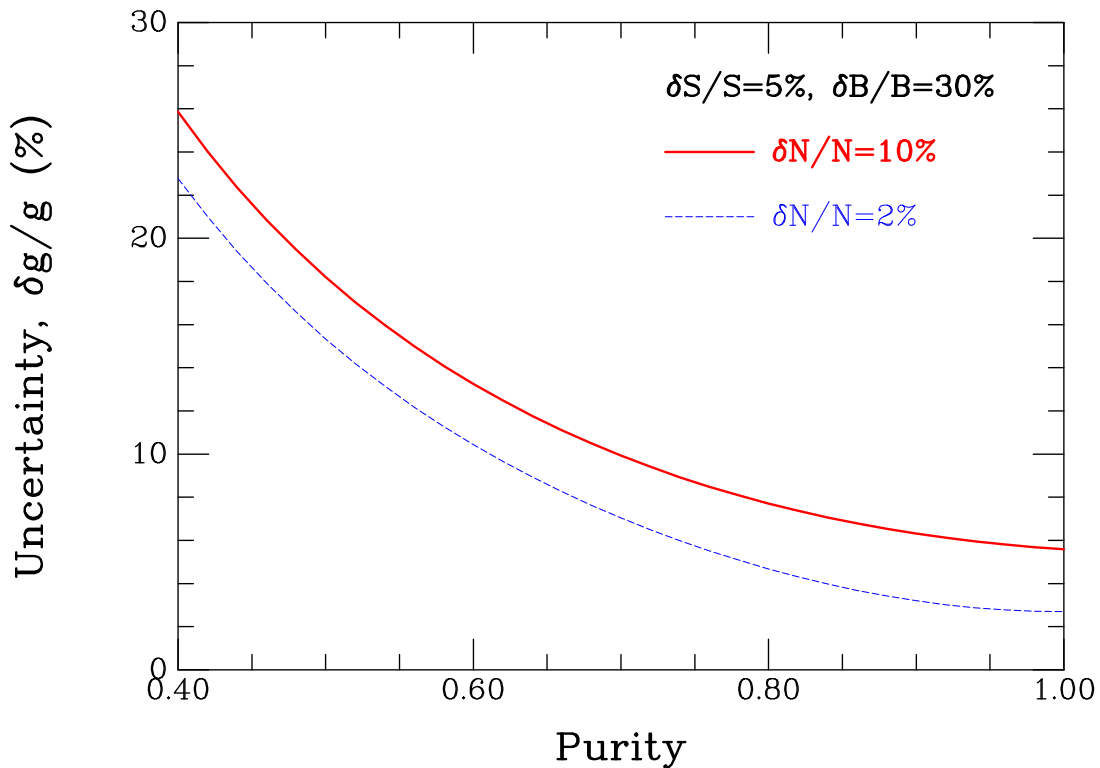
- $(S + B) \sim 12000 \times 0.01 = 120$  events at  
 $m_H = 115$  GeV and  $p_T^{\text{cut}} = 40$  GeV;  
 **$\delta N/N \sim 10\%$**
- $(S + B) \sim 7000 \times 0.036 \sim 250$  events at  
 $m_H = 200$  GeV and  $p_T^{\text{cut}} = 40$  GeV;  **$\delta N/N \sim 6\%$**

## Estimates of Uncertainties in $S$ , $B$ , and $N$

---

- “High luminosity” after 5 years of LHC operation, anticipate an integrated luminosity of  $\sim 200 \text{ fb}^{-1}$ 
  - at  $m_H = 115 \text{ GeV}$  and  $p_T^{\text{cut}} = 40 \text{ GeV}$ ;  
 $\delta N/N \sim 2\%$  in the  $\tau\tau$  mode
  - at  $m_H = 200 \text{ GeV}$  and  $p_T^{\text{cut}} = 40 \text{ GeV}$ ;  
 $\delta N/N \sim 1.5\%$  in the  $WW$  mode

## Coupling Uncertainty vs Signal Purity



- If  $\delta N/N \sim 10\%$      $\delta g/g \sim 10\%$     for  $P = 0.7$
- If  $\delta N/N \sim 2\%$      $\delta g/g \sim 7\%$     for  $P = 0.7$
- Uncertainties in  $S$  and in  $B$  dominate uncertainty in  $g$ .  
 With  $P = 0.7$  and  $\delta N/N = 2\%$ , then  $\delta S/S$  and  $\delta B/B$  have to be reduced to 3% and 6% before statistics control the answer
- $P > 0.65$  permits  $\delta g/g \sim 10\%$  after  $200 \text{ fb}^{-1}$   
 Obtained for  $p_T^{\text{cut}} > 40 \text{ GeV}$  at  $m_H = 115 \text{ GeV}$  and  
 for  $p_T^{\text{cut}} > 20 \text{ GeV}$  at  $m_H = 200 \text{ GeV}$
- Suppose  $K_{\text{background}}^{\text{NLO}} \sim 1.6$   
 $P = 0.56$  for  $p_T^{\text{cut}} > 40 \text{ GeV}$  at  $m_H = 115 \text{ GeV} \rightarrow$   
 $\delta g/g = 13\%$   
 $P = 0.52$  for  $p_T^{\text{cut}} > 20 \text{ GeV}$  at  $m_H = 200 \text{ GeV} \rightarrow$   
 $\delta g/g = 15\%$

## Comparisons with LC Estimates of Couplings

---

- $HZZ$  coupling

- Higgs-strahlung is the dominant production process,  $e^+e^- \rightarrow ZH$ . Once the  $Z$  is identified,  $H$  is discovered in the missing mass distribution. The  $HZZ$  coupling strength is measured independently of the Higgs boson decay products

- Expected accuracy in  $\Delta\sigma_{ZH}/\sigma_{ZH}$

- For  $m_H$  in the range 120 to 160 GeV, Tesla TDR Part III, pp 26-27, quotes an expected statistical accuracy of  $\pm 2.8\%$  ( $e^+e^-$  and  $\mu^+\mu^-$  channels combined), plus  $\pm 2.5\%$  systematics at  $\sqrt{s} = 350$  GeV and  $500\text{fb}^{-1}$
- ALC Working Group Snowmass 2001 Resource Book, p. 120, lists uncertainty of  $6.5\%$  at  $m_H = 120$  GeV, and  $7\%$  at  $m_H = 200$  GeV with  $\sqrt{s} = 500$  GeV and  $500\text{fb}^{-1}$

- Expected accuracy in  $\delta g_{ZZH}/g_{ZZH} \simeq 3\%$

## LC Estimates (continued)

---

- $HW\bar{W}$  coupling
  - Measurement of the  $HW\bar{W}$  coupling is necessary to test the  $SU(2)$  relationship between  $HW\bar{W}$  and  $HZZ$ .
- The usual method relies on the WBF process  $e^+e^- \rightarrow \nu\bar{\nu}H$ , plus knowledge of at least one  $H$  branching fraction. Signals and backgrounds for  $H \rightarrow b\bar{b}$  are studied in detail in Desch and Meyer, LC-PHSM-2001-25 and Brau, Potter, Iwasaki, Snowmass 2001
- Expected accuracy in  $\Delta\sigma_{\nu\bar{\nu}H}/\sigma_{\nu\bar{\nu}H}$ 
  - In the context of the SM, after expected uncertainties on the  $BR(H \rightarrow b\bar{b})$  are included, accuracies of 2.8% to 13% can be obtained for  $m_H$  in the range 120 GeV to 160 GeV at  $\sqrt{s} = 500$  GeV and  $500\text{fb}^{-1}$
- Expected accuracy in  $\delta g_{WWH}/g_{WWH} \simeq 3\%$  to  $\simeq 7\%$
- Knowledge of  $HW\bar{W}$  coupling strength along with  $m_H$  allows one to compute the partial width  $\Gamma_W$ . If an independent measurement of  $BR(H \rightarrow WW^*)$  is also available, the Higgs boson total width  $\Gamma_H$  is obtained:  
$$\Gamma_H = \Gamma_W / BR(H \rightarrow WW^*)$$

## Summary

---

- Studied  $H + 2$  jet production at the energy of the LHC. Fully differential hard matrix elements used to generate  $p_T$  spectra
- Investigated effectiveness of prescriptions to separate/enhance the WBF signal with respect to the irreducible QCD background
- Evaluated the signal purity  $P$  (fraction of real  $H$  events produced by WBF) in each case as a function of the transverse momentum cut used to define the tagging jets
- After  $200 \text{ fb}^{-1}$  are accumulated at the LHC, it may be possible to achieve an accuracy  $\delta g/g \sim 10\%$  in the effective coupling (combination of  $HWW$  and  $HZZ$ ) of the Higgs boson to weak bosons. (These estimates are less optimistic than those in the Les Houches 2003 study)
- With a 500 GeV LC and  $500 \text{ fb}^{-1}$ , the expected accuracies are  $\delta g_{ZZH}/g_{ZZH} \simeq 3\%$  for  $120 < m_H < 200 \text{ GeV}$  and  $\delta g_{WWH}/g_{WWH} \simeq 3\%$  to  $\simeq 7\%$  for  $120 < m_H < 160 \text{ GeV}$



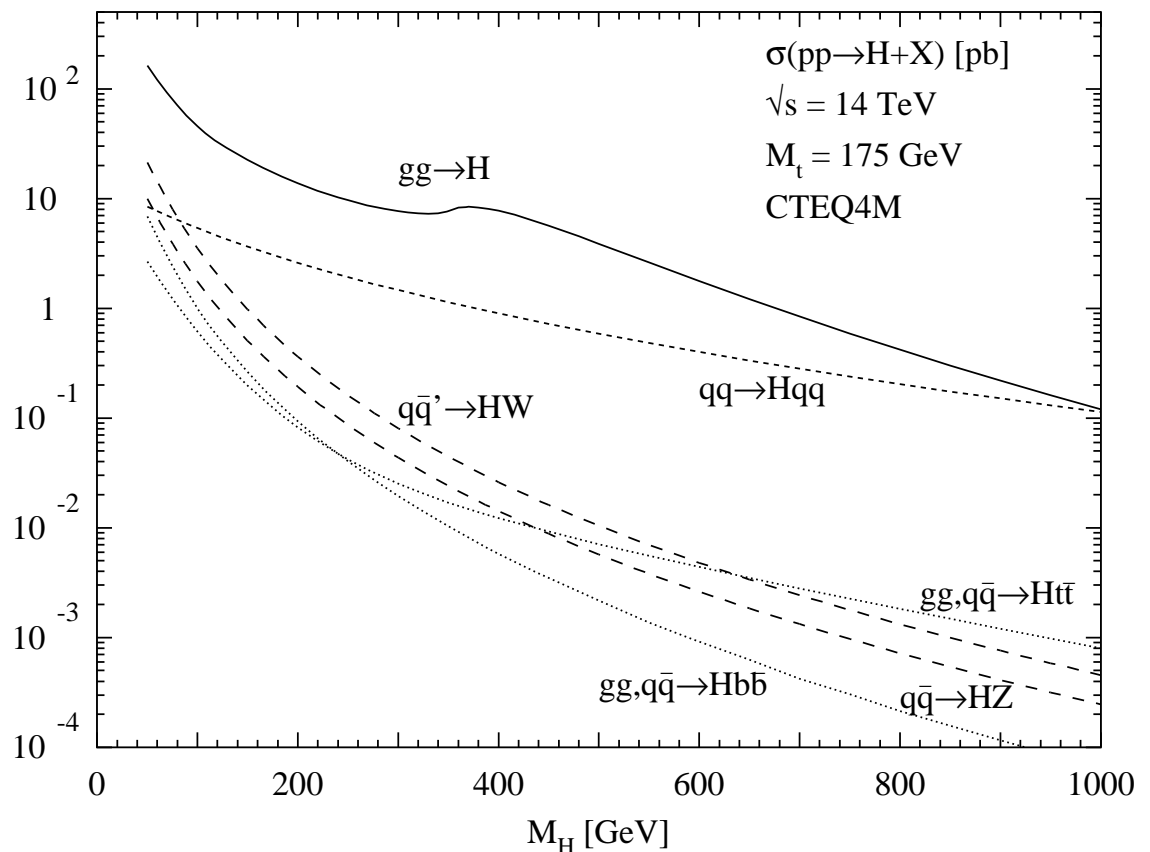
# 1. Introduction and Motivation

- The Higgs boson is expected to be produced at the LHC through various partonic production processes and observed in its decays to SM particles

- $gg \rightarrow hX$ , with  $h \rightarrow \gamma\gamma$ ,  $h \rightarrow WW^*$ ,  $ZZ^*$  ;
- $gg \rightarrow t\bar{t}hX$ , with  $h \rightarrow b\bar{b}$  or  $h \rightarrow \gamma\gamma$  ;
- $qq \rightarrow hqqX$  via  $W^+W^- (ZZ) \rightarrow hX$ , with  $h \rightarrow WW^*$ ,  $h \rightarrow \gamma\gamma$ , or  $h \rightarrow \tau^+\tau^-$

- The fully inclusive gluon-gluon fusion subprocess  $gg \rightarrow hX$  is the dominant production mechanism;  $qq \rightarrow H + 2 \text{ jets}$  is next in line

(figure from M. Spira)



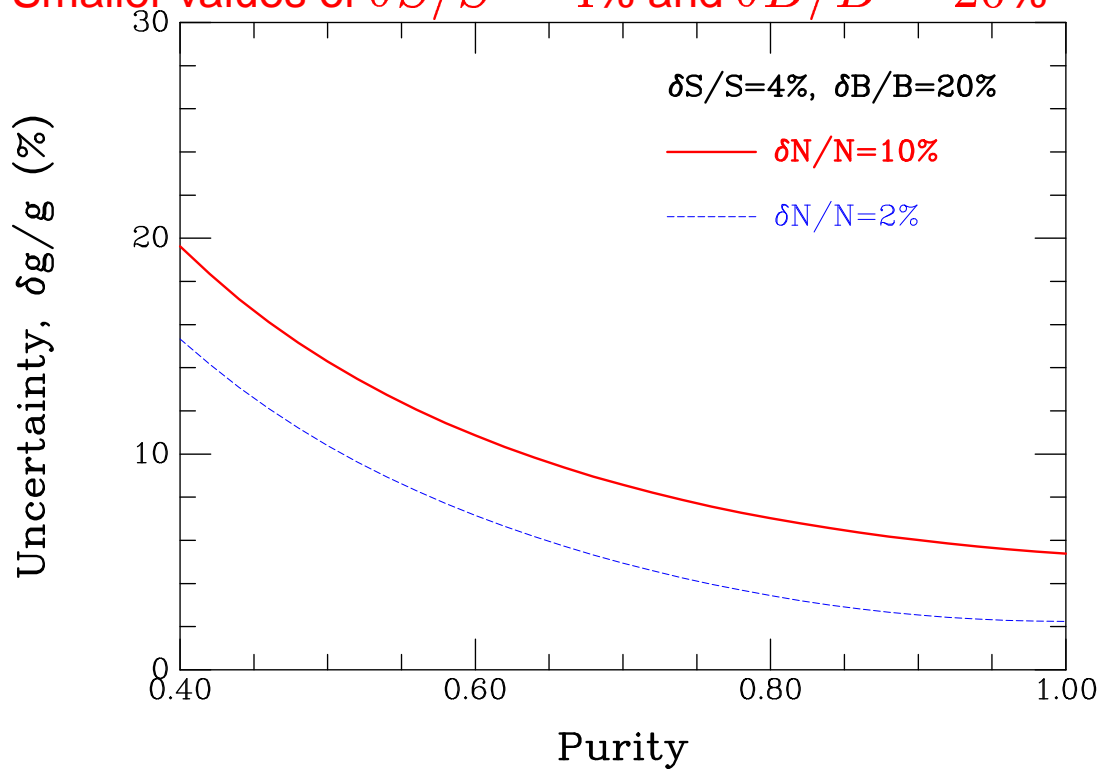
## Generic Cuts

---

- Generic cuts Figy et al. Jets from the Monte Carlo runs are clustered according to the  $k_T$  algorithm with
  - $p_T^{\text{jet}} > 20 \text{ GeV}$ , **to be raised**
  - jet pseudo-rapidity  $|\eta^{\text{jet}}| < 4.5$ , and
  - jet separation  $\Delta R_{jj} = \sqrt{\Delta\eta_{jj}^2 + \Delta\phi_{jj}^2} > 0.8$
- The two jets with the highest  $p_T$  are chosen as the tagging jets and ordered in rapidity,  $\eta_{j_1} < \eta_{j_2}$
- To approximate the acceptance for the Higgs boson decay products imagine a Higgs boson decay to two charged particles, denoted “leptons”
  - Require  $p_T^{\text{lept}} > 20 \text{ GeV}$ ,  $|\eta^{\text{lept}}| < 2.5$ ,  
 $\Delta R_{j\ell} > 0.6$ ,  $\eta_{j_1} < \eta_{\text{lept}} < \eta_{j_2}$
- Higgs decay products lie between the tagging jets

## Coupling Uncertainty vs Signal Purity

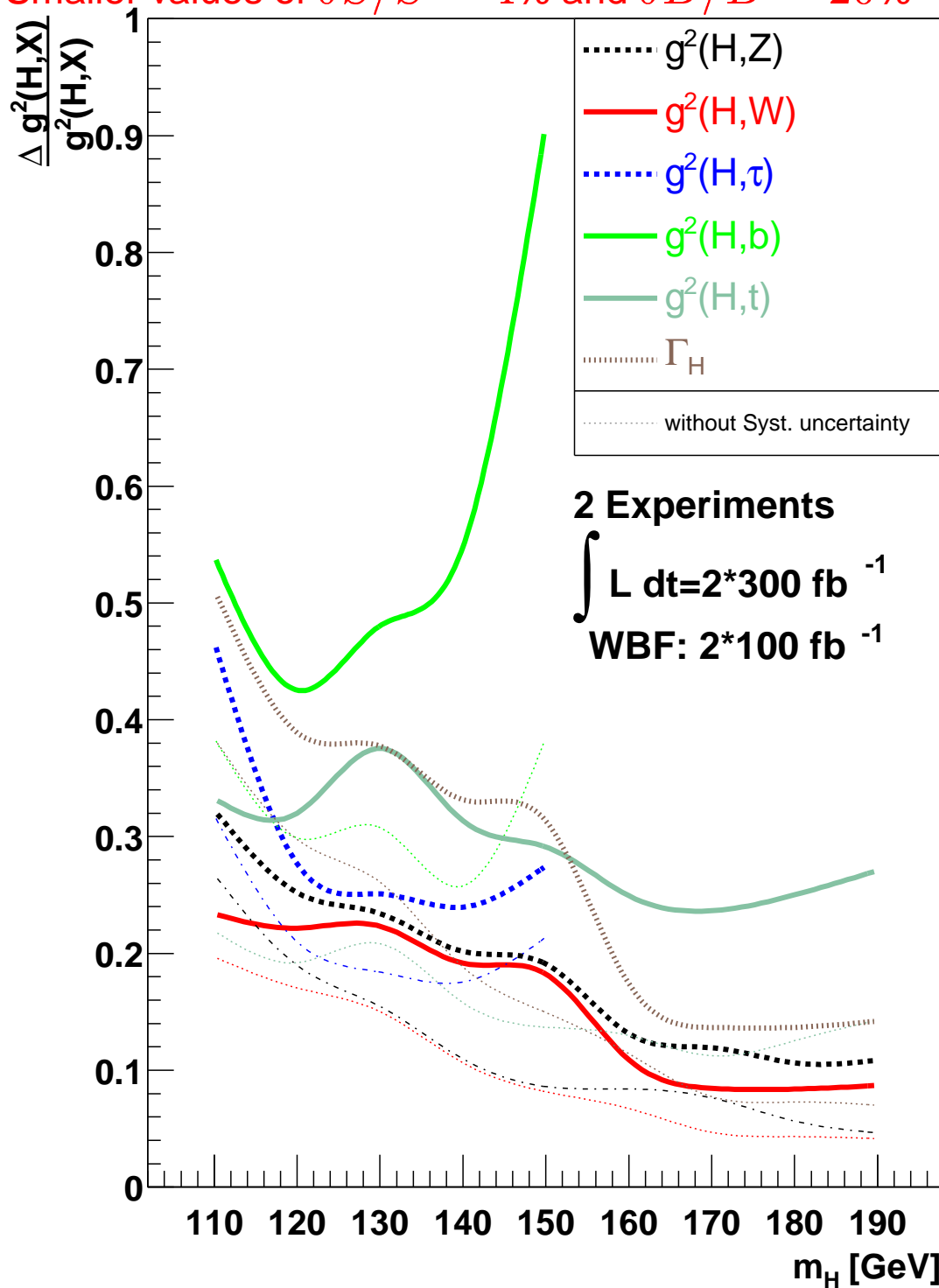
- Smaller values of  $\delta S/S = 4\%$  and  $\delta B/B = 20\%$



- If  $\delta N/N \sim 10\%$      $\delta g/g \sim 9\%$     for  $P = 0.7$
- If  $\delta N/N \sim 2\%$      $\delta g/g \sim 5\%$     for  $P = 0.7$
- New lower values of  $\delta g/g$  are very similar to Düehrsen et al, Les Houches 2003 for comparable luminosity
- Not evident from these figures that there is much to gain from  $P > 0.7$

# Coupling Uncertainty vs Les Houches Results

- Smaller values of  $\delta S/S = 4\%$  and  $\delta B/B = 20\%$



- Scope of the Les Houches study is more ambitious, but the WBF results at high luminosity are quite similar

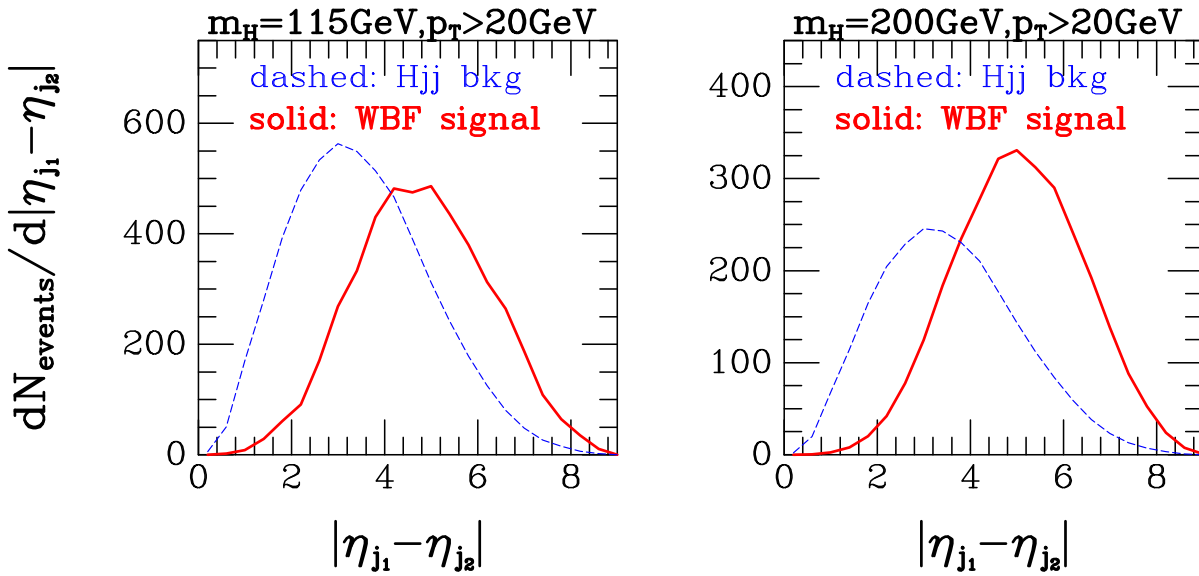
## 4. Alternative WBF Prescriptions

---

- We use the requirement that at least one jet have  $1.6 < |\eta| < 4.4$
- A different prescription requires instead a rapidity separation requirement  $|\eta_{j1} - \eta_{j2}| > 4$
- Another requires an invariant mass cut  $M_{jj} > 800 \text{ GeV}$   
→ Figures and Tables
- With these alternatives, there is a significant gain in  $P$  for  $p_T^{\text{cut}} = 20 \text{ GeV}$ , but not for larger values. The gain is accompanied by loss in signal rate at all  $p_T$
- Potential advantages of simple cut on  $|\eta|$  of one jet in a high luminosity environment
  - In data (and at higher orders in QCD) there are several jets; our prescription may be easier to implement
  - In a high luminosity environment, with more than one event per beam crossing, selection on only one jet (plus the  $H$ ) reduces chance that jets from different events are used
- Full experimental simulation would be useful. One could begin with hard QCD LO  $H + 2 \text{ jet}$  matrix elements plus Pythia showering – improvement over current ATLAS studies (c.f., S. Asai et al hep-ph/0402254)

# $H + 2 \text{ Jet Production} - \text{Jet Rapidity Separation}$

- Higgs boson  $H$  production via  $WW$  scattering in NLO and via  $gg$  QCD processes (LO) (for  $1 \text{ fb}^{-1}$ )



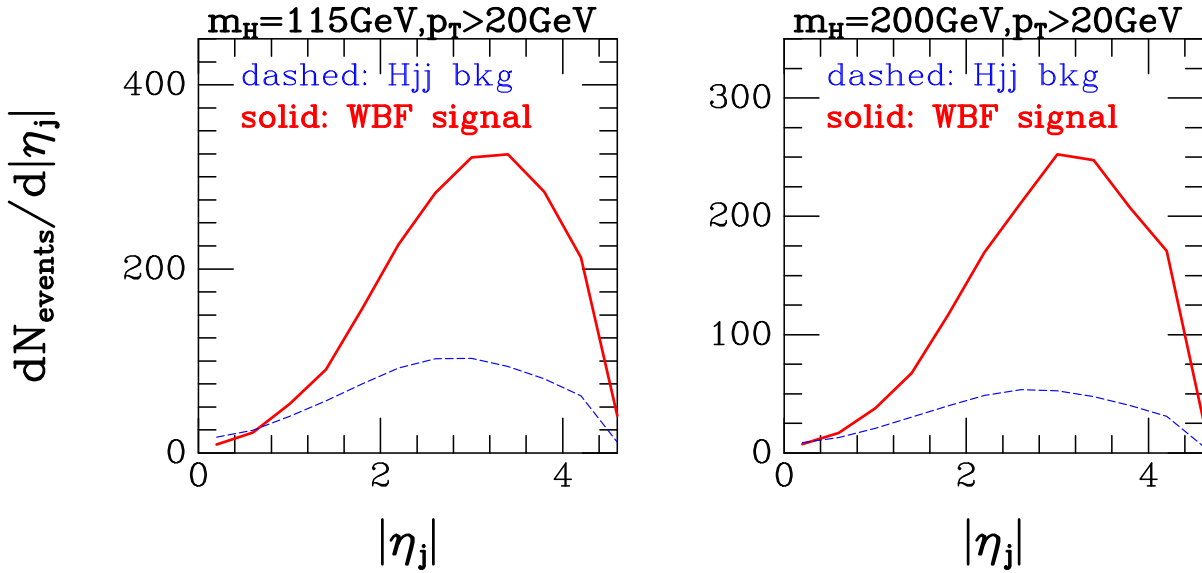
- Shape motivates a rapidity separation cut

$$|\eta_{j1} - \eta_{j2}| > 4$$

$p_T$ cut [GeV]	20	40	80
Signal ( $m_H = 115$ )	1297	718	137
Bkg	758	207	38
Purity	0.63	0.78	0.78
Signal ( $m_H = 200$ )	911	521	106
Bkg	349	102	20
Purity	0.72	0.84	0.84

## $H + 2$ Jet Production – Jet Rapidity with Mass Cut

- Higgs boson  $H$  production via  $WW$  scattering in NLO and via  $gg$  QCD processes (LO) (for  $1 \text{ fb}^{-1}$ )



- Alternative WBF prescription:

$$M_{jj} > 800 \text{ GeV}$$

$p_T$ cut [GeV]	20	40	80
Signal ( $m_H = 115$ )	808	561	158
Bkg	304	183	82
Purity	0.73	0.75	0.66
Signal ( $m_H = 200$ )	617	428	121
Bkg	157	95	43
Purity	0.80	0.82	0.74